

to the horizontal with the initial velocity v_0 . Assuming the air drag to be negligible, find:
 (a) the time of motion;
 (b) the maximum height of ascent and the horizontal range; at what value of the angle α they will be equal to each other;
 (c) the equation of trajectory $y(x)$, where y and x are displacements of the body along the vertical and the horizontal respectively;
 (d) the curvature radii of trajectory at its initial point and at its peak.

• 1.30. Using the conditions of the foregoing problem, draw the approximate time dependence of moduli of the normal w_n and tangent w_t acceleration vectors, as well as of the projection of the total acceleration vector w on the velocity vector direction.

• 1.31. A ball starts falling with zero initial velocity on a smooth inclined plane forming an angle α with the horizontal. Having fallen the distance h , the ball rebounds elastically off the inclined plane. At what distance from the impact point will the ball rebound for the second time?

• 1.32. A cannon and a target are 5.10 km apart and located at the same level. How soon will the shell launched with the initial velocity 240 m/s reach the target in the absence of air drag?

• 1.33. A cannon fires successively two shells with velocity $v_0 = 250$ m/s; the first at the angle $\theta_1 = 60^\circ$ and the second at the angle $\theta_2 = 45^\circ$ to the horizontal, the azimuth being the same. Neglecting the air drag, find the time interval between firings leading to the collision of the shells.

• 1.34. A balloon starts rising from the surface of the Earth. The ascension rate is constant and equal to v_0 . Due to the wind the balloon gathers the horizontal velocity component $v_x = ay$, where a is a constant and y is the height of ascent. Find how the following quantities depend on the height of ascent:
 (a) the horizontal drift of the balloon $x(y)$;
 (b) the total, tangential, and normal accelerations of the balloon.

• 1.35. A particle moves in the plane xy with velocity $\mathbf{v} = ai + b\tau j$, where i and j are the unit vectors of the x and y axes, and a and b are constants. At the initial moment of time the particle was located at the point $x = y = 0$. Find:
 (a) the equation of the particle's trajectory $y(x)$;
 (b) the curvature radius of trajectory as a function of x .

• 1.36. A particle A moves in one direction along a given trajectory with a tangential acceleration $w_t = a\tau$, where a is a constant vector coinciding in direction with the x axis (Fig. 1.4), and τ is a unit vector coinciding in direction with the velocity vector at a given point. Find how the velocity of the particle depends on x provided that its velocity is negligible at the point $x = 0$.

• 1.37. A point moves along a circle with a velocity $v = at$, where $a = 0.50$ m/s². Find the total acceleration of the point at the mo-

ment when it covered the n -th ($n = 0.10$) fraction of the circle after the beginning of motion.

• 1.38. A point moves with deceleration along the circle of radius R so that at any moment of time its tangential and normal accelerations



Fig. 1.4.

are equal in moduli. At the initial moment $t = 0$ the velocity of the point equals v_0 . Find:

(a) the velocity of the point as a function of time and as a function of the distance covered s ;

(b) the total acceleration of the point as a function of velocity and the distance covered.

• 1.39. A point moves along an arc of a circle of radius R . Its velocity depends on the distance covered s as $v = a\sqrt{s}$, where a is a constant. Find the angle α between the vector of the total acceleration and the vector of velocity as a function of s .

• 1.40. A particle moves along an arc of a circle of radius R according to the law $l = a \sin \omega t$, where l is the displacement from the initial position measured along the arc, and a and ω are constants. Assuming $R = 1.00$ m, $a = 0.80$ m, and $\omega = 2.00$ rad/s, find:

(a) the magnitude of the total acceleration of the particle at the points $l = 0$ and $l = \pm a$;

(b) the minimum value of the total acceleration w_{min} and the corresponding displacement l_m .

• 1.41. A point moves in the plane so that its tangential acceleration $w_t = a$, and its normal acceleration $w_n = bt^4$, where a and b are positive constants, and t is time. At the moment $t = 0$ the point was at rest. Find how the curvature radius R of the point's trajectory and the total acceleration w depend on the distance covered s .

• 1.42. A particle moves along the plane trajectory $y(x)$ with velocity v whose modulus is constant. Find the acceleration of the particle at the point $x = 0$ and the curvature radius of the trajectory at that point if the trajectory has the form

(a) of a parabola $y = ax^2$;

(b) of an ellipse $(x/a)^2 + (y/b)^2 = 1$; a and b are constants here.

• 1.43. A particle A moves along a circle of radius $R = 50$ cm so that its radius vector \mathbf{r} relative to the point O (Fig. 1.5) rotates with the constant angular velocity $\omega = 0.40$ rad/s. Find the modulus of the velocity of the particle, and the modulus and direction of its total acceleration.